

1. The computed value of F is $f = \frac{MSTr}{MSE} = \frac{2673.3}{1094.2} = 2.44$. Degrees of freedom are $I - 1 = 4$ and $I(J - 1) = (5)(3) = 15$. From Table A.9, $F_{.05,4,15} = 3.06$ and $F_{.10,4,15} = 2.36$; since our computed value of 2.44 is between those values, it can be said that $.05 < P\text{-value} < .10$. Therefore, H_0 is not rejected at the $\alpha = .05$ level. The data do not provide statistically significant evidence of a difference in the mean tensile strengths of the different types of copper wires.

3. With $\mu_i =$ true average lumen output for brand i bulbs, we wish to test $H_0 : \mu_1 = \mu_2 = \mu_3$ v. H_a : at least two μ_i 's are different. $MSTr = \hat{\sigma}_B^2 = \frac{591.2}{2} = 295.60$, $MSE = \hat{\sigma}_W^2 = \frac{4773.3}{21} = 227.30$, so

$$f = \frac{MSTr}{MSE} = \frac{295.60}{227.30} = 1.30.$$

For finding the P -value, we need degrees of freedom $I - 1 = 2$ and $I(J - 1) = 21$. In the 2nd row and 21st column of Table A.9, we see that $1.30 < F_{.10,2,21} = 2.57$, so the P -value $> .10$. Since $.10$ is not $< .05$, we cannot reject H_0 . There are no statistically significant differences in the average lumen outputs among the three brands of bulbs.

11. $Q_{.05,5,15} = 4.37$, $w = 4.37 \sqrt{\frac{272.8}{4}} = 36.09$. The brands seem to divide into two groups: 1, 3, and 4; and 2 and 5; with no significant differences within each group but all between group differences are significant.

3	1	4	2	5
437.5	462.0	469.3	512.8	532.1
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12. Brands 2 and 5 do not differ significantly from one another, but both differ significantly from brands 1, 3, and 4. While brands 3 and 4 do differ significantly, there is not enough evidence to indicate a significant difference between 1 and 3 or 1 and 4.

3	1	4	2	5
427.5	462.0	469.3	512.8	532.1
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24. Let μ_i denote the true average skeletal-muscle activity the i th group ($i = 1, 2, 3$). The hypotheses are $H_0: \mu_1 = \mu_2 = \mu_3$ versus H_a : at least two of the μ_i 's are different.

From the summary information provided, $\bar{x}_.. = 51.10$, from which

$$SSTr = \sum_{i=1}^3 \sum_{j=1}^{J_i} (\bar{x}_i - \bar{x}_..)^2 = \sum_{i=1}^3 J_i (\bar{x}_i - \bar{x}_..)^2 = 797.1. \text{ Also, } SSE = \sum_{i=1}^3 \sum_{j=1}^{J_i} (\bar{x}_{ij} - \bar{x}_i)^2 = \sum_{i=1}^3 (J_i - 1) s_i^2 = 1319.7. \text{ The}$$

numerator and denominator df are $I - 1 = 2$ and $n - I = 28 - 3 = 25$, from which the F statistic is

$$f = \frac{MSTr}{MSE} = \frac{797.1/2}{1319.7/25} = 7.55.$$

Since $F_{.01,2,25} = 5.57$ and $F_{.001,2,25} = 9.22$, the P -value for this hypothesis test is between .01 and .001. There is strong evidence to suggest the population mean skeletal-muscle activity for these three groups is not the same.

To compare a group of size 10 to a group of size 8, Tukey's "honestly significant difference" at the .05

level is $w = Q_{.05,3,25} \sqrt{\frac{MSE}{2} \left(\frac{1}{10} + \frac{1}{8} \right)} \approx 3.53 \sqrt{\frac{52.8}{2} \left(\frac{1}{10} + \frac{1}{8} \right)} = 8.60$. So, the "old, active" group has a

significantly higher mean s-m activity than the other two groups, but young and old, sedentary populations are not significantly different in this regard.

Young	Old sedentary	Old active
46.68	47.71	58.24