

11. $(\bar{x} - \bar{y}) \pm z_{\alpha/2} \sqrt{\frac{s_1^2}{m} + \frac{s_2^2}{n}} = (\bar{x} - \bar{y}) \pm z_{\alpha/2} \sqrt{(SE_1)^2 + (SE_2)^2}$. Using $\alpha = .05$ and $z_{\alpha/2} = 1.96$ yields $(5.5 - 3.8) \pm 1.96 \sqrt{(0.3)^2 + (0.2)^2} = (0.99, 2.41)$. We are 95% confident that the true average blood lead level for male workers is between 0.99 and 2.41 higher than the corresponding average for female workers.

13. $\sigma_1 = \sigma_2 = .05$, $d = .04$, $\alpha = .01$, $\beta = .05$, and the test is one-tailed \Rightarrow

$$n = \frac{(.0025 + .0025)(2.33 + 1.645)^2}{.0016} = 49.38, \text{ so use } n = 50.$$

18.

- a. Let μ_1 and μ_2 denote true mean CO₂ loss with a traditional pour and a slanted pour, respectively. The hypotheses of interest are $H_0: \mu_1 - \mu_2 = 0$ v. $H_a: \mu_1 - \mu_2 \neq 0$. We'll apply the two-sample t procedure,

$$\text{with } \nu = \frac{(.5^2/4 + .3^2/4)^2}{(.5^2/4)^2/(4-1) + (.3^2/4)^2/(4-1)} = 4.91 \rightarrow 4. \text{ The test statistic is } t = \frac{(4.0 - 3.7) - 0}{\sqrt{\frac{.5^2}{4} + \frac{.3^2}{4}}} = 1.03,$$

with a two-sided P -value of roughly $2(.187) = .374$ from Table A.8. [Software provides the more accurate P -value of .362.] Hence, we fail to reject H_0 at any reasonable significance level; we conclude that there is no statistically significant difference in mean "bubble" loss between traditional and slanted champagne pouring, when the temperature is 18°C.

- b. Repeating the process of **a** at 12°C, we have $\nu \approx 5$, $t = 7.21$, P -value $\approx 2(0) = 0$. [Software gives $P = .001$]. Hence, we reject H_0 at any reasonable significance level; we conclude that there is a statistically significant difference in mean "bubble" loss between traditional and slanted champagne pouring, when the temperature is 12°C.

24.

- a. 95% upper confidence bound: $\bar{x} + t_{.05, 65-1} SE = 13.4 + 1.671(2.05) = 16.83$ seconds

- b. Let μ_1 and μ_2 represent the true average time spent by blackbirds at the experimental and natural locations, respectively. We wish to test $H_0: \mu_1 - \mu_2 = 0$ v. $H_a: \mu_1 - \mu_2 > 0$. The relevant test statistic is

$$t = \frac{13.4 - 9.7}{\sqrt{2.05^2 + 1.76^2}} = 1.37, \text{ with estimated df} = \frac{(2.05^2 + 1.76^2)^2}{\frac{2.05^4}{64} + \frac{1.76^4}{49}} \approx 112.9. \text{ Rounding to } t = 1.4 \text{ and}$$

df = 120, the tabulated P -value is very roughly .082. Hence, at the 5% significance level, we fail to reject the null hypothesis. The true average time spent by blackbirds at the experimental location is not statistically significantly higher than at the natural location.

- c. 95% CI for silvereyes' average time - blackbirds' average time at the natural location: $(38.4 - 9.7) \pm (2.00) \sqrt{1.76^2 + 5.06^2} = (17.96 \text{ sec}, 39.44 \text{ sec})$. The t -value 2.00 is based on estimated df = 55.

28. We will test the hypotheses: $H_0: \mu_1 - \mu_2 = 10$ v. $H_a: \mu_1 - \mu_2 > 10$. The test statistic is

$$t = \frac{(\bar{x} - \bar{y}) - 10}{\sqrt{\left(\frac{2.75^2}{10} + \frac{4.44^2}{5}\right)}} = \frac{4.5}{2.17} = 2.08 \text{ with df} = \nu = \frac{\left(\frac{2.75^2}{10} + \frac{4.44^2}{5}\right)^2}{\frac{(2.75^2)^2}{9} + \frac{(4.44^2)^2}{4}} = \frac{22.08}{3.95} = 5.59 \searrow 5, \text{ and the } P\text{-value from}$$

Table A.8 is $\approx .045$, which is $< .10$ so we reject H_0 and conclude that the true average lean angle for older females is more than 10 degrees smaller than that of younger females.

36. From the data provided, $\bar{d} = 7.25$ and $s_D = 11.8628$. The parameter of interest: $\mu_D =$ true average difference of breaking load for fabric in unabraded or abraded condition. The hypotheses are $H_0: \mu_D = 0$ versus $H_a: \mu_D > 0$. The calculated test statistic is $t = \frac{7.25 - 0}{11.8628/\sqrt{8}} = 1.73$; at 7 df, the P -value is roughly .065. Since $.065 > .01$, we fail to reject H_0 at the $\alpha = .01$ level. The data do not indicate a significant mean difference in breaking load for the two fabric load conditions.
40. From the data, $n = 10$, $\bar{d} = 105.7$, $s_D = 103.845$.
- Let $\mu_D =$ true mean difference in TBBMC, postweaning minus lactation. We wish to test the hypotheses $H_0: \mu_D \leq 25$ v. $H_a: \mu_D > 25$. The test statistic is $t = \frac{105.7 - 25}{103.845/\sqrt{10}} = 2.46$; at 9 df, the corresponding P -value is around .018. Hence, at the 5% significance level, we reject H_0 and conclude that true average TBBMC during postweaning does exceed the average during lactation by more than 25 grams.
 - A 95% upper confidence bound for $\mu_D = \bar{d} + t_{.05,9}s_D/\sqrt{n} = 105.7 + 1.833(103.845)/\sqrt{10} = 165.89$ g.
 - No. If we pretend the two samples are independent, the new standard error is is roughly 235, far greater than $103.845/\sqrt{10}$. In turn, the resulting t statistic is just $t = 0.45$, with estimated df = 17 and P -value = .329 (all using a computer).