## Statistics 512: Homework#5 Due February 28, 2014 BEFORE CLASS

For the following problems use the computer science data that we have been discussing in class. You can get a copy of the data set csdata.dat from the class website. The variables are: id, a numerical identifier for each student; GPA, the grade point average after three semesters; HSM; HSS; HSE; SATM; SATV, which were all explained in class; and GENDER, coded as 1 for men and 2 for women.

- 1. In this exercise you will illustrate some of the ideas described in Chapter 7 of the text related to the extra sums of squares.
  - (a) Create a new variable called SAT which equals SATM + SATV and run the following two regressions:
    - i. predict GPA using HSM, HSS, and HSE;
    - ii. predict GPA using SAT, HSM, HSS, and HSE.

Calculate the extra sum of squares for the comparison of these two analyses. Use it to construct the F-statistic – in other words, the general linear test statistic – for testing the null hypothesis that the coefficient of the SAT variable is zero in the model with all four predictors. What are the degrees of freedom for this test statistic?

- (b) Use the test statement in proc reg to obtain the same test statistic. Give the statistic, degrees of freedom, *p*-value and conclusion.
- (c) Compare the test statistic and *p*-value from the test statement with the individual *t*-test for the coefficient of the SAT variable in the full model. Explain the relationship.
- 2. Run the regression to predict GPA using SATM, SATV, HSM, HSE, and HSS. Put the variables in the order given above in the model statement. Use the SS1 and SS2 options in the model statement.
  - (a) Add the Type I sums of squares for the five predictor variables. Do the same for the Type II sums of squares. Do either of these sum to the model sum of squares? Are there any predictors for which the two sums of squares (Type I and Type II) are the same? Explain why.
  - (b) Verify (by running additional regressions and doing some arithmetic with the results) that the Type I sum of squares for the variable SATV is the difference in the model sum of squares (or error sum of squares) for the following two analyses:
    - i. predict GPA using SATM, SATV;
    - ii. predict GPA using SATM.
- 3. Create an additional variable called HS that is the sum of the three high school scores (HSE + HSS + HSM). Run the regression to predict GPA using a variety of variables, including HS and SAT, as described below. Summarize the results by making a table giving the percentage of variation explained  $(R^2)$  by each of the following models:
  - (a) SATM as the explanatory variable
  - (b) SATV as the explanatory variable
  - (c) HSM as the explanatory variable

- (d) HSS as the explanatory variable
- (e) HSE as the explanatory variable
- (f) SATM and SATV as the explanatory variables
- (g) SAT (=SATM+SATV) as the explanatory variable
- (h) HSM, HSS, and HSE as the explanatory variables
- (i) HS (=HSM+HSS+HSE) as the explanatory variable
- (j) SATM, SATV, HSM, HSS, and HSE as the explanatory variables
- (k) SAT and HS as the explanatory variables

(Please do not include the SAS output for all these models. Only the  $R^2$  value is needed. Note that you can run proc reg with multiple model statements to save typing.)