## STAT 350 Exam 2: Practice Exam

### Spring 2016

Name (Print) :		PUID		
Instructor (circle one):	Findsen	Monter	Tooman	Womble
Class Time (circle one):	9:30 am	11:30 AM	12:30 PM	
• • •	1:30 PM	2:30 PM	3:30 PM	ONLINE

#### Instructions:

- 1. You are expected to uphold the honor code of Purdue University. It is your responsibility to keep your work covered at all times. Anyone cheating on the exam will automatically fail the course and will be reported to the Office of Dean of Students.
- 2. Please let us know if you observe or hear of any cheating on the exam. We highly appreciate it and will reward your efforts with one bonus point per instance.
- 3. It is strictly prohibited to smuggle this exam outside. Your exam will be returned to you (online: you may pick up your exam from your instructor) after it is graded.
- 4. You may have one double-sided 8.5 in x 11 in crib sheet to take this test. The crib sheet can be handwritten or typed.
- 5. The only materials that you are allowed during the exam are your calculator, writing utensils, erasers and your crib sheet. If you bring any other papers into the exam, you will get a **zero** on the exam. Scratch paper will be provided if you need more room.
- 6. Leave all your belongings except those permitted for the exam in the front of the room. This includes your cell phone. We are not responsible for any loss.
- 7. If you share your calculator or use a cell phone, you will get a **zero** on the exam.
- 8. Breaks (including bathroom breaks) during the exam are **not** allowed. If you leave the exam room, you must turn in your exam and you will not be allowed to come back.
- 9. You must show **ALL** your work to obtain full credit. An answer without showing any work may result in **zero** credit.
- 10. All numeric answers should have **two decimal places** except answers from the z-table which should have **four decimal places**.
- 11. If your work is not readable, it will be marked wrong.
- 12. After you complete the exam, please turn in your exam as well as your crib sheet, tables and any scrap paper that you used. Please put your name on all pages that are stapled to the exam. Please be prepared to show your Purdue picture ID.

#### Your exam is not valid without your signature below.

I attest here that I have read and followed the instructions above honestly while taking this exam and that the work submitted is my own, produced without assistance from books, other people (including other students in this class), notes other than my own crib sheets, or other aids. In addition, I agree that if I tell any other student in this class anything about the exam BEFORE they take it, I (and the student that I communicate the information to) will fail the course and be reported to the Office of the Dean of Students for Academic Dishonesty.

Signature of Student: \_\_\_\_\_

	Points Earned	Grader
Name/Section/Signature (1 point)		
Problem 1 (Multiple Choice) (39 points)		
Problem 2 (32 points)		
Problem 3 (25 points)		
Problem 4 (20 points)		
Problem 5 (40 points)		
<del>Total (105 / 100 )</del>		

Note: There 156 points on the exam, however, the midterm will be out of 105/100.

# 1. (39 points, 3 points each) Multiple Choice Questions (<u>circle</u> only one answer). If you do not circle the answer, you will receive 0 points for the question. There is only one correct answer per question.

- 1.1 A random sample of 35 koalas was obtained and each was carefully weighed. The average weight was 20.75 pounds and the sample standard deviation was 3.05. A 99% confidence interval for the population mean weight of all koalas is (19.422, 22.078). Determine which of the following statements is true:
  - A. Researches are 99% confident that the CI captures the population mean.
  - B. Researches are 99% confident that the population mean lies in the CI.
  - C. Researches are 99% confident that the CI captures the sample mean.
  - D. Researches are 99% confident that the sample mean lies in the CI.
- 1.2 Determine which of the following statements is true concerning a hypothesis test:
  - A. If *p*-value >  $\alpha$  we have strong evidence to accept H<sub>0</sub>
  - B. The *p*-value is the probability that  $H_0$  is true.
  - C. Small *p*-values are evidence against H<sub>0</sub>
  - D. Large *p*-values give convincing evidence against H<sub>0</sub>
- 1.3 The average time in years to get an undergraduate degree in computer science was compared for men and women. Random samples of 100 male computer science majors and 100 female computer science majors were taken. Choose the appropriate parameter(s) for this situation.
  - A. One population mean  $\mu_1$
  - B. Difference between two population means  $\mu_1 \mu_2$  where they are independent.
  - C. Difference between two population means  $\mu_1 \mu_2$  where they are paired.
  - D. None of the above.
- 1.4 Null and alternative hypotheses are statements about:
  - A. Population parameters.
  - B. Sample parameters.
  - C. Sample statistics.
  - D. It depends sometimes population parameters and sometimes sample statistics.
- 1.5 A pitcher in the MLB wants to know the mean speed of his pitch for the last season. The head coach tells him that the 90% confidence upper bound for his mean pitching speed is 99.23 mph. He wishes to test H<sub>0</sub>:  $\mu$ = 105 mph versus H<sub>a</sub>:  $\mu$  < 105 mph at the 1% significance level. Determine which of the following statements is true.
  - A. The 99% confidence upper bound is less than the 90% confidence upper bound.
  - B. We reject H<sub>0</sub> since the value 105 falls out of the 90% confidence upper bound and would therefore also fall out of the 99% confidence upper bound.
  - C. We fail to reject because the 90% confidence upper bound is smaller than 105.
  - D. We cannot make a decision since the confidence level we used to calculate the confidence upper bound is 90%, and we would need a 99% confidence upper bound.

- 1.6 A good way of determining the proper alternative hypothesis for a hypothesis test is to evaluate
  - A. what parameter value(s) the experimenter assumes to be true without proof.
  - B. what the experimenter is trying to prove or detect about the parameter(s) being tested.
  - C. what the experimenter claims to be a valid value for the parameter being tested.
  - D. the likely consequence should  $H_0$  be proven false.
- 1.7 To optimize the Atlanta bus service, the average number of minutes that busses in each of 20 randomly selected bus routes is late (compared to the published time) was recorded. You may assume that the times follow a normal distribution with an unknown mean  $\mu$  and unknown standard deviation  $\sigma$ . Which of the following would produce a confidence interval with a smaller half-width than a 95% confidence interval?
  - A. Compute a 99% confidence interval rather than a 95% confidence interval so that you are more confident of the result.
  - B. Record 10 bus routes rather than 20, because 10 routes are easier to measure.
  - C. Select bus routes that do not go through downtown to decease variability.
  - D. Select bus routes to those routes that are less than 10 miles so that the average time of the route is shorter.
- 1.8. To be sure that a computer supply store is refilling their generic replacement ink cartridges to 30 mL of ink, a consumer group randomly sampled 17 black replacement cartridges. The results of the test stated that the ink was less than 30 mL to a 0.01 level of significance. Suppose that in reality, the amount of ink in the cartridges was 30 mL or more. Which of the following statements is TRUE?
  - A. A Type I error has been committed.
  - B. A Type II error has been committed.
  - C. No error has been committed.
- 1.9. Which of the following is **NOT** true about the standard error of a statistic?
  - A. The standard error measures, roughly, the average difference between the statistic and the population parameter.
  - B. The standard error is the estimated standard deviation of the sampling distribution for the statistic.
  - C. The standard error can never be a negative number.
  - D. The standard error increases as the sample size(s) increases.
- 1.10 A professor wishes to record information on some of his upper division students for later use. He randomly chooses five juniors and five seniors from his class. What best describes his sampling technique?
  - A. SRS
  - B. stratified random sample design
  - C. matched pair design
  - D. block design
- 1.11 Which of the following should **NOT** be considered when designing an experiment:

- 1.12A behavioral scientist wishes to know more about the walking habits of university students across a particular campus sidewalk. She positions herself out of sight of the students who are walking and records the time required for several of them to pass between two fixed points along the sidewalk. Which of the following best describes this study?
  - A. anecdote
  - B. observational study
  - C. experiment with a control
  - D. experiment with no control
- 1.13 A study was conducted to compare five different training programs for improving endurance. Forty subjects were randomly divided into five groups of eight subjects in each group. A different training program was assigned to each group. After 2 months, the improvement in endurance was recorded for each subject. A one-way ANOVA is used to compare the five training programs, and the resulting *p*-value is 0.014. At a significance level of 0.05, what is the appropriate conclusion about mean improvement in endurance?
  - A. The average amount of improvement appears to be the same for all five training programs.
  - B. It appears that at least one of the five training programs has a different average amount of improvement.
  - C. The average amount of improvement appears to be different for each of the five training programs.
  - D. One training program is significantly better than the other four.

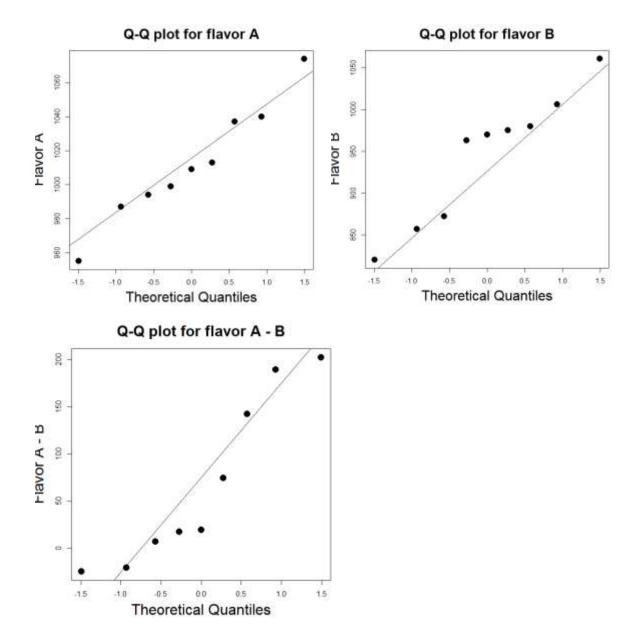
- (32 pts.) 2. The director of a High School is concerned about how much time students spent on homework. Last year, the average time students spent on homework was 21 hours per week. This year, a random sample of 32 students indicates that the average time spent is 22.4 hours per week. Assume that the population standard deviation is 2.7 hours.
  - a. (5 pts.) What assumptions are required for this test to be valid?
  - b. (5 pts.) Is this a z or a t test? Please explain your answer.
  - c. (10 pts.) Perform the 4 step hypothesis test to determine whether there is any evidence to suggest that students spent more time on homework this year than last year. Please use a significance level of 1%.

- d. (7 pts.) Construct a 99% lower confidence bound for the population mean. No interpretation is required
- e. (5 pts.) Explain why parts c) and d) are consistent with each other.

(25 pts.) 3. An experiment was run to determine whether or not different flavors of ice cream melt at different speeds. Two flavors, A and B, of ice cream were stored in the same freezer in similar-sized containers. For each observation, one teaspoonful of ice cream was taken from the freezer, transferred to a plate, and the melting time at room temperature was observed to the nearest second. Nine observations were taken on each flavor. These are shown in the following table, and the normal probability plots of these data are shown below.

Flavor	Time in Seconds							Mean	SD		
А	1009	987	955	1074	994	1040	1037	999	1013	1012	34.7
В	820	970	980	872	975	1061	963	857	1006	944.9	78.2
A - B	189	17	-25	202	19	-21	74	142	7	67.1	89.0

The calculated degrees of freedom using the Satterthwaite approximation is 11.03.



a. (5 points) Should you use the two sample independent or two-sample pairs procedure to analyze the data? Explain your answer. You will receive a **0** points if the reason relates to the data that is provided in the question.

b. (5 pts.) Using the graphs provided, are the assumptions met to perform the inference? Please explain your answer. Be sure to indicate which graphs you are using.

c. (10 points) No matter what your answer is in b), construct and interpret a 95% confidence interval for the mean difference in melting time for the two flavors. Remember, we will grade on consistency from part a).

d. (5 points) Please write an English sentence stating whether you think that these two flavors of ice cream melt in the same amount of time. To help in your decision, it is not possible to determine differences of melting times of less than 10 seconds

- (20 points) 4. A cosmetics manufacturer of a hairspray product states that their product has a hold time of 24 hours. To test this claim, we randomly sample 30 people who use the hairspray and obtained a sample mean hold time 18.4 hours with a sample standard deviation of 5.4 hours.
  - a. (10 pts.) Construct a 95% confidence interval for the length of time that the hairspray holds. Be sure to interpret your interval.

b. (5 pts.) Using the preliminary information provided in the question, what approximate sample size is required so that the half-width of the confidence interval is at most 1.5 hours with a confidence level of 95%?

c. (5 pts.) Without performing the hypothesis test, is the manufacture's claim correct at a 5% significance level? Explain your answer. You will receive **0 points** if your explanation includes the calculation of the test statistic or the P value.

(40 points) 5. The weight gain of women during pregnancy has an important effect on the birth weight of their children. If the weight gain is not adequate, the infant is more likely to be small and will tend to be less healthy. In a study conducted in three countries, weight gains (in kilograms) of women during the third trimester of pregnancy were measured. The results are summarized in the following table:

Country	Ν	Mean	StDev	
Egypt	46	3.7	2.5	
Kenya	100	3.1	1.8	
Mexico	52	2.9	1.8	
Analysis of Varian	се			
Source	SS	MS	F-Value	P-Value
Country(Model)	17.22	8.61	XXX	0.1321
Error	767.25	XXXX		

a (5 pts.) Is it reasonable to use the assumption of equal standard deviation when analyzing these data? Give a reason for your answer.

b. (5 pts.) Find the value of MSE. What is the standard deviation?

- c. (5 pts.) What are the numerator and denominator degrees of freedom for the F statistic?
- d. (5 pts.) Find the value of the F statistic.

e. (10 pts.) Carry out a significance test to compare the mean birth weights for the three countries at a significance level 0.05. Please follow the four step procedure and <u>make a conclusion in context</u>.

- f. (5 pts.) Should a multiple comparison test be performed in this situation? Please explain your answer in one sentence.
- g. (5 pts.) No matter what your answer is in the previous question, what would be the critical value and Standard Error using the Tukey multiple comparison method? If the conclusion in part e) was reject, the following question would be asked: What would be the smallest weight gain during pregnancy? Please explain your answer. A listing of the confidence intervals would be included.