



Statistics based upon data

EDA: Exploratory Data Analysis

(Tukey)

- Learning from Data
- What can the data tell you?
- Show me your problems?
- Show me your data?
- Tell me how were the data collected?
- What can the data tell you (& how)?



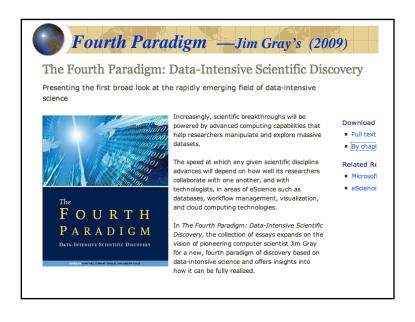


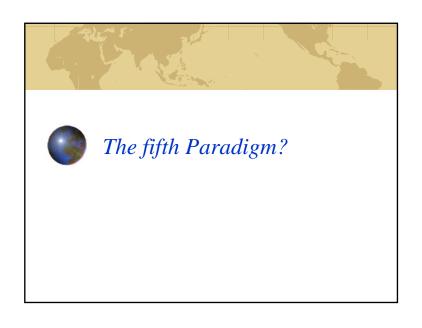
Where did Data come from?

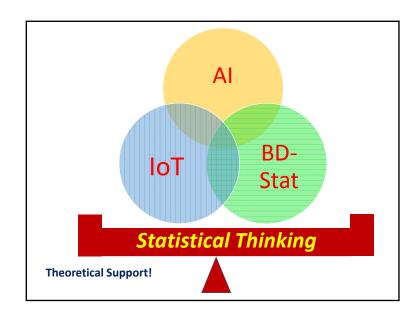


Scientist(s) analyze(s) database / files

Access crucial







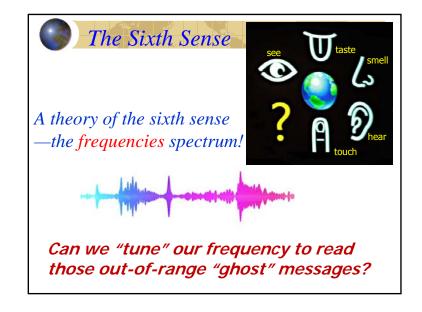




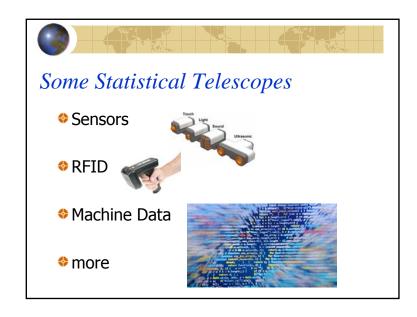


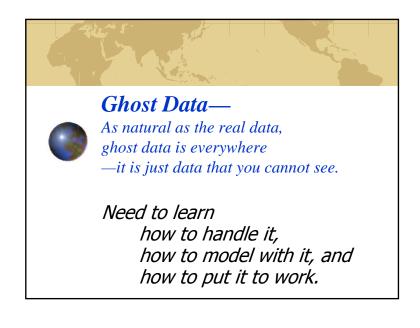






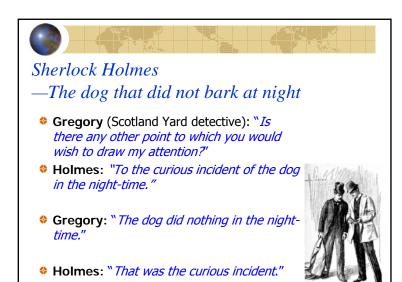


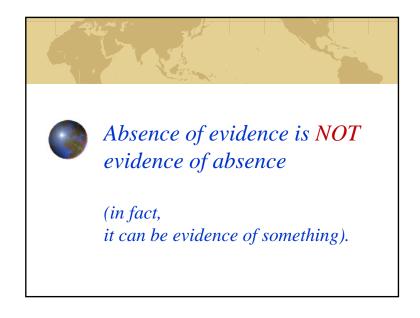


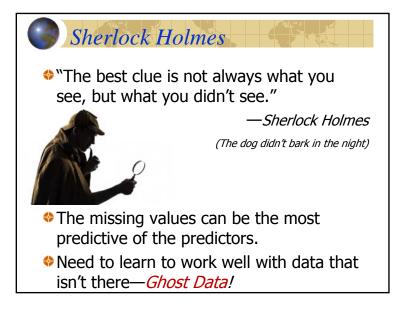
















Absence of Expected Facts

Expected—model based Absence—data based

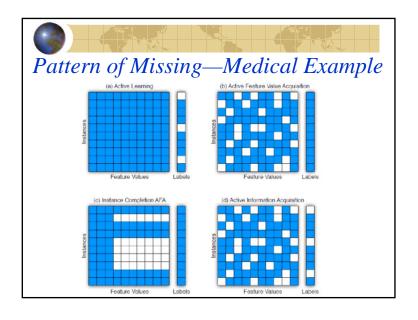


Don Rubin (1972, *Biometrika*)
Special Issue of *Statistica Sinica* (2018)



When a student receives "0" in her/his exam...this could be

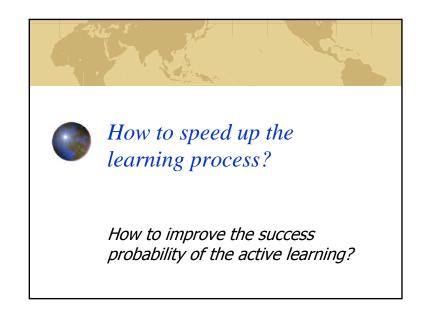
- Did come & hand in Exam, and indeed get a "0"
 Not a missing
- Did not come to Exam
 - Missing in Action
- Did come & hand in Exam, but get lost in process
 Missing at Random
- Did come but did not hand in Exam
 Missing Not at Random
- etc













- The Sixth Sense
 - I can see things that you cannot see
- Sherlock Holmes
 - absence of expected facts
- Edge of Tomorrow
 - how to speed up your learning





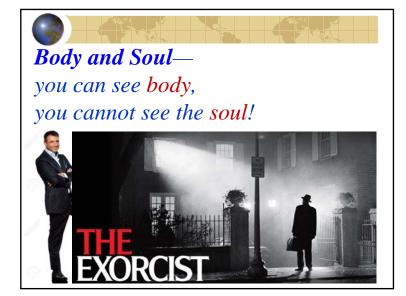




Statistical Microscope

- You have to decide What to see, and How to see?
- The power of DoE (Design of Experiment)

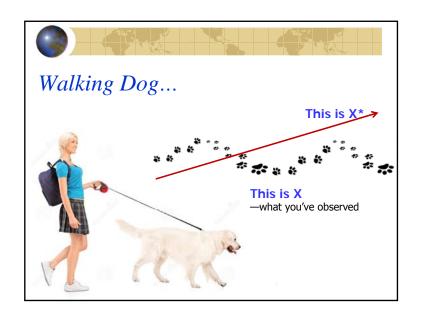


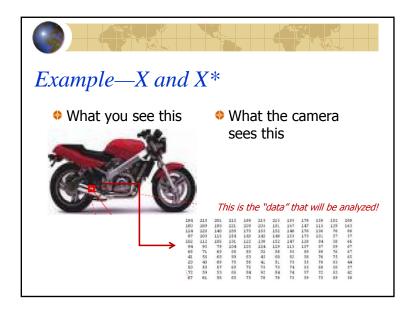


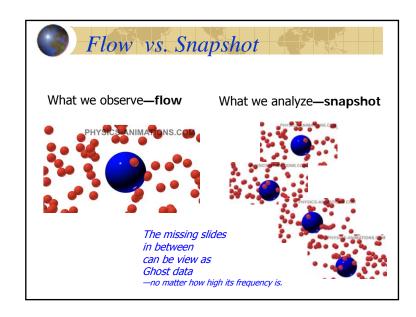


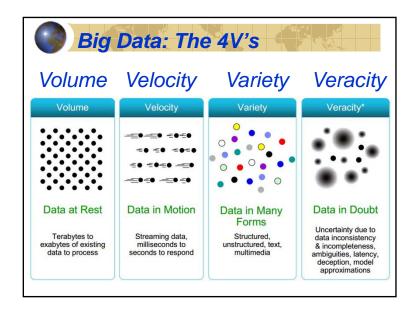
X is what you "observed" (body), while X* is the "truth" (soul-ghost)!

- X=X* lucky you!
- X is X* "plus" some kind of noises
 X=X*+Δ or X=X*•δ, or any other form
- X is a low-dimension projection of X*
- X is a "transformation" of X*Confidentiality/privacy Data
- X is empty (while X* is not)









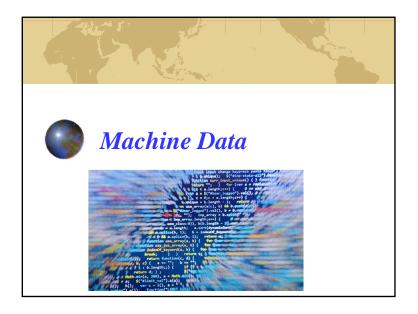


Variety: New Types of Data

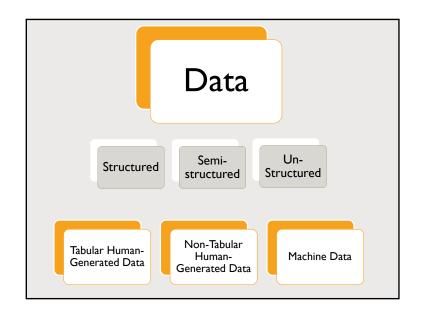
- Text Data
- Audio Data
- Image Data
- Video Data
- Social Media Data
- Network Data

Stock ...

- Finger Print Data
- Citation Data (ranking/rating)
- etc...







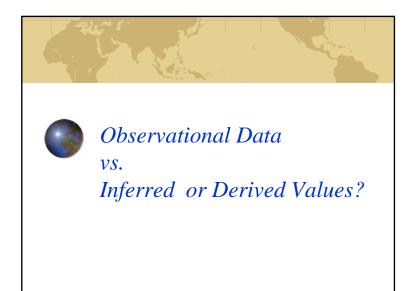


Why Don't Traditional models fit?

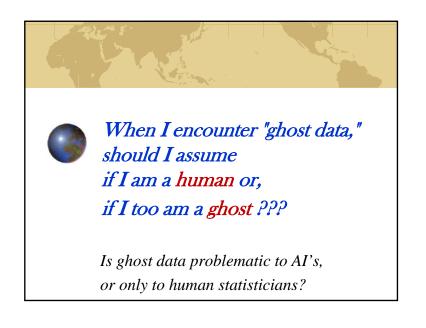
Data Structure

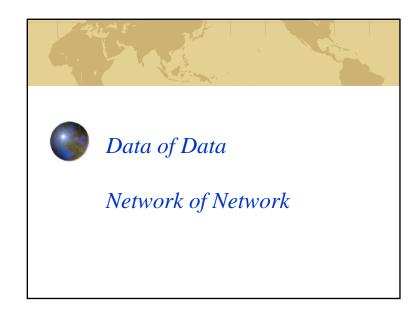
- Traditional data is structured
- Machine data is a mix of data structure types
- **Data Complexity**
- Loses the ability to present a simple and clear picture of nature's mechanism
- Too complex to fit to a pre-existing model

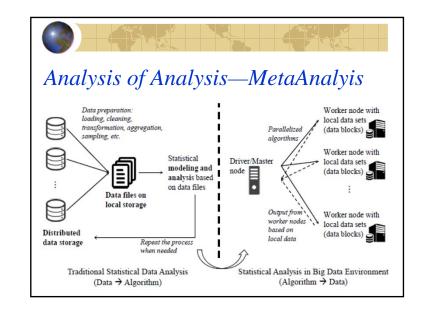


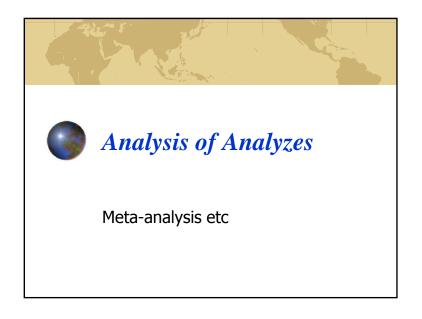














Ghost Data—examples

It is as natural as real data. It's just data that isn't there.

(John Sall)

- ♦ Virtual data (虚拟数据)
 - Virtual Reality—it isn't there until you look at it;
- ♦ Missing data (缺失数据)
 - there is a slot to hold a value, but the slot is empty;
- ◆ Pretend data (做作数据)
 - data that is made up;
- ♦ Simulation data (模拟数据)
 - data to answer "what if."
- ♦ Highly Sparse Data (高度稀疏数据)
 - whose absence implies a zero



Are they i.i.d. Normal???

If so, I have a lots to offer...

Central Limit Theorem, Asymptotical Normality,
Law of Large Number, etc.

If not...well...



Ghost Data—some extensions

- Optimization via Simulation
- Partition Model
- Two-Stage Least Squares Estimate
- Hidden Markov Chain
- Adversarial Learning
- Topological data
- Feature engineering
- Unknown tuning parameters



Ghost Data for Industrial Statistics

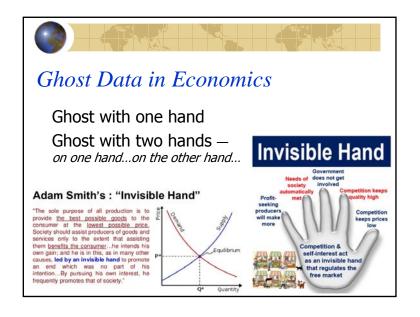
- Design of Experiment
 - Decide what to see and how to see?

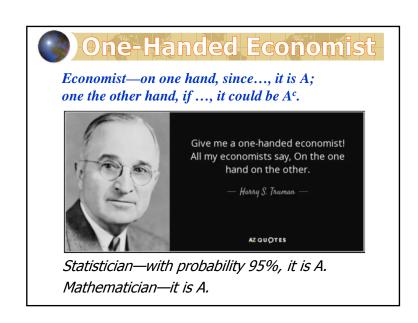


- What we see is "dead" (failures), but what we are interested in is "alive".
- Control Charts
 - How to monitoring Ghost data? (Ghost Hunting—TV series)









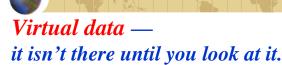




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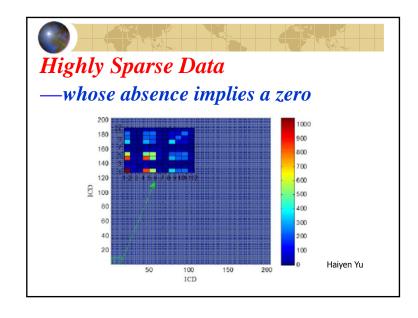
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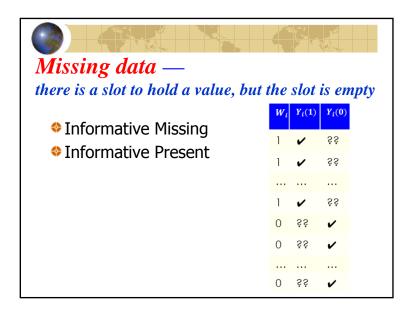


- Movie Plus Game
 - Have to decide what to see —design of experiment
 - Design and Analysis of Virtual Reality Data
- Detect whether there is a bug—software reliability (see Kevin Quinlan, t-covering)
- Compact Urban Cell











Notations

- Y: incomplete variable
- R: response indicator
 - \mathbb{R} R = 1 if Y is observed; R=0 otherwise
- X: fully observed covariate
- Y_{obs} and Y_{mis}: the observed and missing parts of Y



Missing (not) At Random

Imputation under MAR (Missing at Random)

$$P(Y|X,R = 0) = P(Y|X,R = 1)$$

Imputation under MNAR (Missing Not at Random)

$$P(Y|X,R = 0) \neq P(Y|X,R = 1)$$



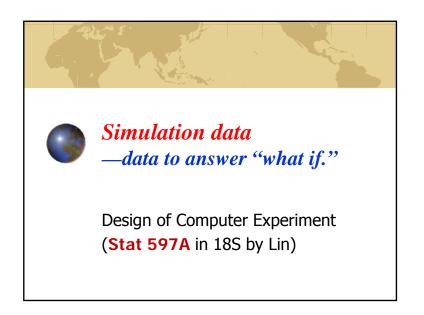
Government data— public data under protection (confidentiality)

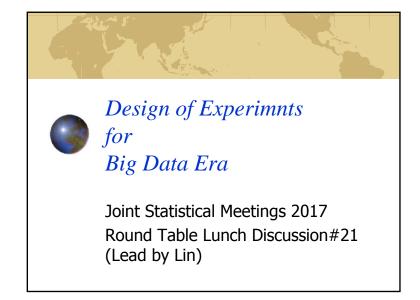
- Lin in Advisory Board for
 - Bureau of Statistics (Taiwan) &
 - State Bureau of Statistics (China) since 1998.
- There is Statistics Canada, but there is no Bureau of Statistics in USA—try NISS!

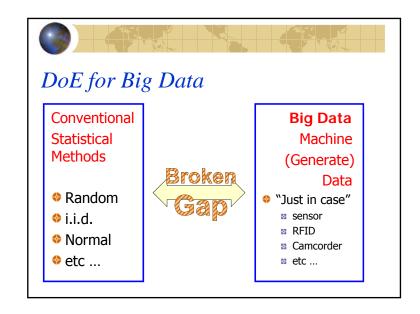


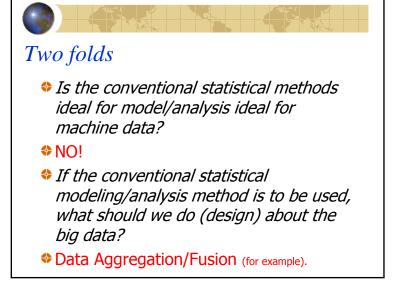
Pretend data — data that is made up

Under Construction!











Large Data Set

Statistics: n>30

Comp Sci: n>30GB (or even 30TB)

Dimension Reduction

Statistics: from d=10 into d=2Comp Sci: from $d=10^{10}$ to $d=10^2$.

Ultra High-Dimension

Statistics: d=50

Comp Sci: d=10¹² =1,000,000,000,000

Fast Computing

Statistics: from $O(n^{1/4})$ to $O(n^{1/5})$

Comp Sci: from 20 minutes to 6 seconds ($4G \rightarrow 5G$).

