

1. Suppose the underlying process  $Y(s)$ ,  $s \in [-1, 1]$  has a known mean 0 and a spherical covariogram with range 0.8

$$C(h) = 1 - 1.5(h/0.8) + 0.5(h/0.8)^3, \text{ if } h < 0.8$$

and equals 0 if  $h \geq 0.8$ . The following function calculates the spherical covariogram:

```
cov.spher=function(x, theta){
  v=theta[1]
  phi=theta[2]
  x[x>phi]=phi
  1-1/5*(x/phi)+0.5*(x/phi)^3
}
```

We observe the process at 40 locations:  $j/20$  for  $j = \pm 1, \pm 2, \dots, \pm 20$  and predict  $Y(0)$ .

- Calculate the 40 simple kriging coefficients. You may obtain the coefficients using matrix-vector operations or a R package such as `geoR` or `gstat`.
  - Plot the coefficients against the sampling locations.
  - You will find that the prediction is influenced by not only two the two adjacent locations:  $\pm 1/20$ , but also some locations far away such as  $\pm 17/20$  and  $\pm 15/20$ . Is this desirable?
2. Repeat Problem 1 for the squared spherical covariogram  $C(h)^2$ . Now, which locations are practically influential to the prediction of  $Y(0)$ ? Which covariogram, the spherical or the squared spherical, would you prefer?