

Week 7, Thursday - Topics for Exam 1  
 Office hours Tuesday of  
 October break 11-12 or appt.  
 4 questions, multiple parts  
 2 questions, EMS

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Hypothesis test.  
 Layout & Model.  
 1. Hypotheses  
 2. test statistic (SNR)  
 3. p-value - measure of significance  
 4. Conclusion:  
     reject  $H_0$   
     do not reject  $H_0$

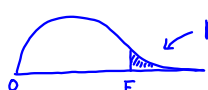
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t-test  
 Independent sample &  
 paired data.  
 Type I error -  $\alpha = \Pr(\text{false})$   
 Type II error -  $\beta = \Pr(\text{do not detect effect})$   
 Power =  $1 - \beta$

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One-way ANOVA (fixed effect model)  
 Randomization  
 Layout & Model  
 Hypothesis test

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Hypothesis test  
 $H_0: \mu_i = \mu_j \text{ all } i, j$   
 $H_a: \mu_i \neq \mu_j \text{ some } i, j$   
 $F = \frac{MS_{Treat}}{MS_{Error}}$   


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Post F-test analysis.  
 If reject  $H_0$ , need to compare cell means.  
 Options:  
 1) No prior information, so compare all pairs of means.

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Range test for all means comparisons.

- Experimentwise procedure  
 $\alpha = \text{Pr}(\text{make any Type I error})$
- Comparisonwise  
 $\alpha = \text{Pr}(\text{any one comp. gives Type I error})$

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More powerful - Comparisonwise but more likely to make Type I error.  
 Bonferroni Ineq.

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2) Orthogonal Contrasts - Have prior information which suggests certain comparisons.  
 example 1: Control, Trt1, Trt2  
 Prior: Trt1 + 2 should be same

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C	T <sub>1</sub>	T <sub>2</sub>
xx x	xx x	xx x
0	-1	1
1	-1/2	-1/2
<hr/>		
0.1	+ 1/2	- 1/2 = 0

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Common mistake.

	A	hi	hi	lo	lo
Main A	-1	-1	1	1	
Main B	-1	1	-1	1	
AB	1	-1	-1	1	

Pairwise!

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3) Dunnett's test - Have true control group. Compare all trt's to control

C	T <sub>1</sub>	T <sub>2</sub>	T <sub>3</sub>

Experimentwise

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Diagnostics -  
 Equality of variances  
 Plot

Res. ← usual problem  
 Pred.

- Test  
 Equal Variance  
 Bartlett's  
 Levene's

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2nd most common problem,  
 "ceiling" or "floor" effects.  
 Test, one group gets ~100%  
 another scores near 0.

res  
 pred.

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Normality  
 plot - Normal plot, q-q plot.  
 Test of normality -  
 Shapiro-Wilks test.

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If my assumption not  
 satisfied, then we transform  
 the data. Box-Cox transformation  
 usually solves the problem.

redo ANOVA  
 means comparisons  
 diagnostics.

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Two-way ANOVA  
 Layout + Model

$Y_{ijk} = \mu + A_i + B_j + AB_{ij} + \epsilon_{(ijk)}$

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Complete, balanced, factorial design:

- ↑ all combinations of factors
- ↑ same # obs/cell
- ↑ means factors crossed

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Three situations:

- 1) Fixed model, both factors fixed
- 2) Mixed model, one fixed one random
- 3) Random model, both factors random.

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Fixed model:

Test interaction, if significant do range test on cell means. If not significant, test Main effects + do range test on signif. main effects.

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Mixed Model: A fixed, B random

Source	df	EMS
A <sub>i</sub>		$\sigma_e^2 + n\sigma_{AB}^2 + nb\phi_A$
B <sub>j</sub>		$\sigma_e^2 + na\sigma_B^2$
AB <sub>ij</sub>		$\sigma_e^2 + n\sigma_{AB}^2$
error		$\sigma_e^2$

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If A significant, do range test Comparing levels of A.  
If B or AB significant, estimate  $\sigma_B^2$  or  $\sigma_{AB}^2$ .

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Random effects: Test all terms, estimate  $\sigma_A^2, \sigma_b^2$  or  $\sigma_{AB}^2$  if F-test was significant.

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Do diagnostics always!

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Three-way ANOVA  
Layout, model, EMS, correct F-tests.

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